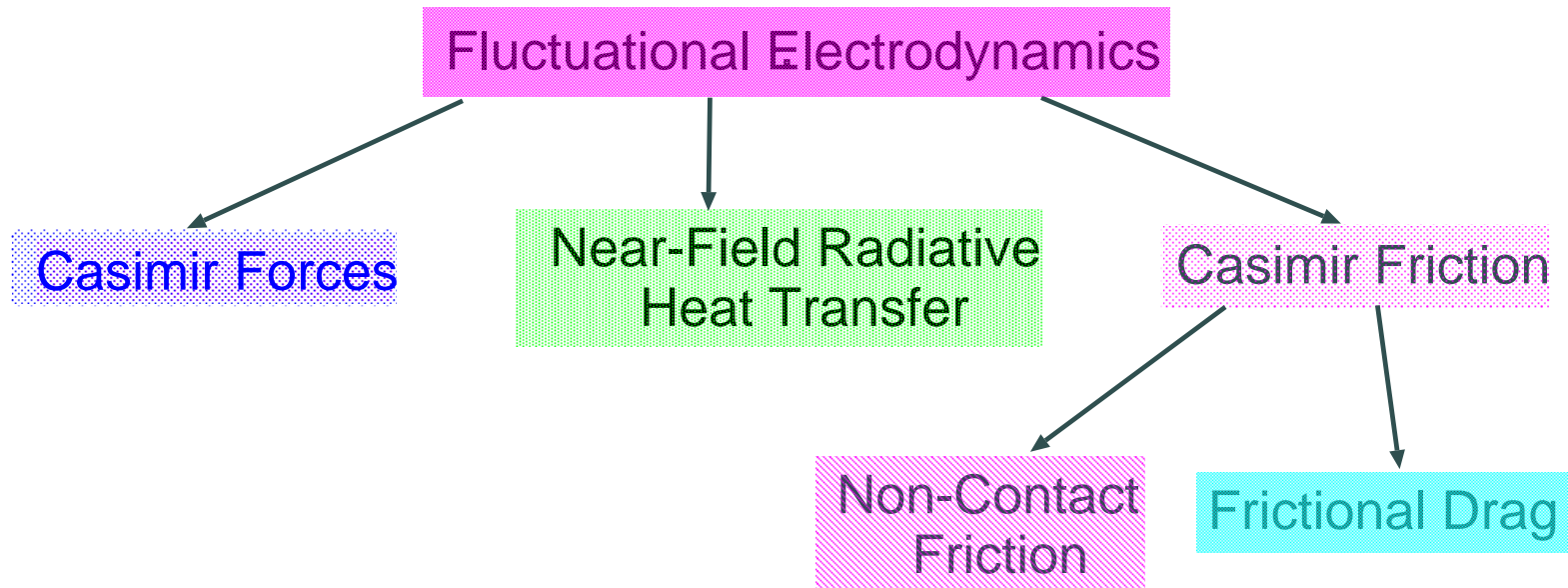


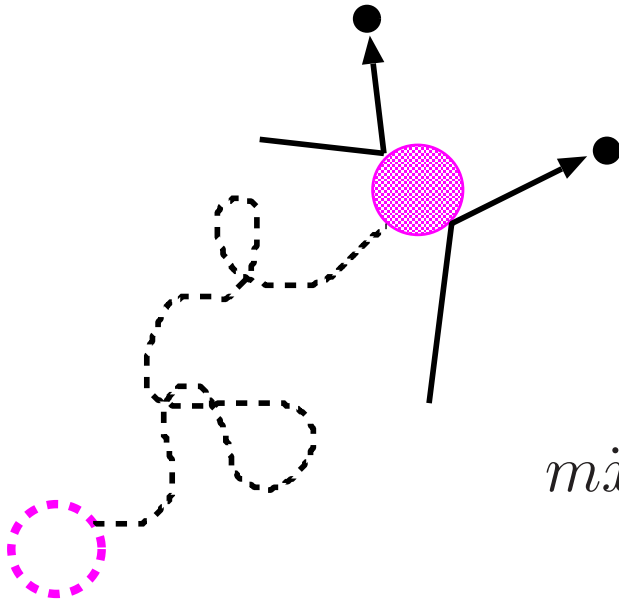
Casimir Friction

Aleksandr Volokitin

Research Center Jülich and Samara State Technical University



Fluctuation-Dissipation Theorem

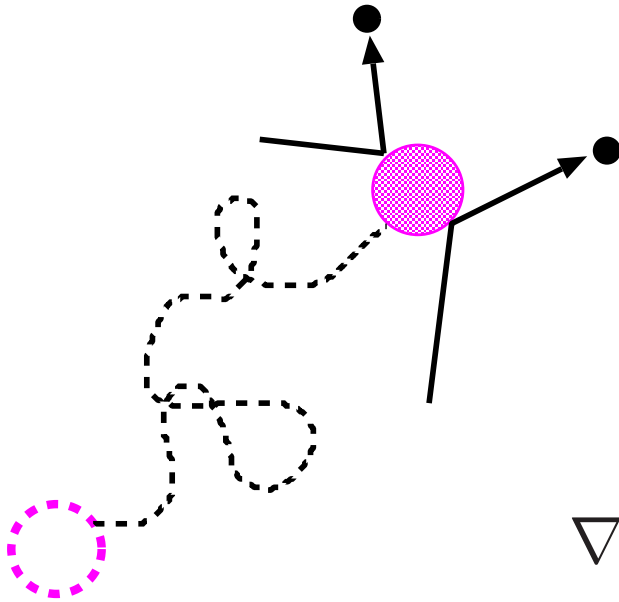


$$m\ddot{x} + m\omega_0^2 x + \Gamma\dot{x} = F(t)$$

$$\Gamma = (k_B T)^{-1} \text{Re} \int_0^\infty dt \langle \hat{\mathbf{F}}(t) \hat{\mathbf{F}}(0) \rangle$$

- The detection of single spins by MRFM for: (a) 3D atomic imaging (b) quantum computation
- Measurements of gravitation force at short length scale
- Measurements of Casimir forces

Rytov's Theory



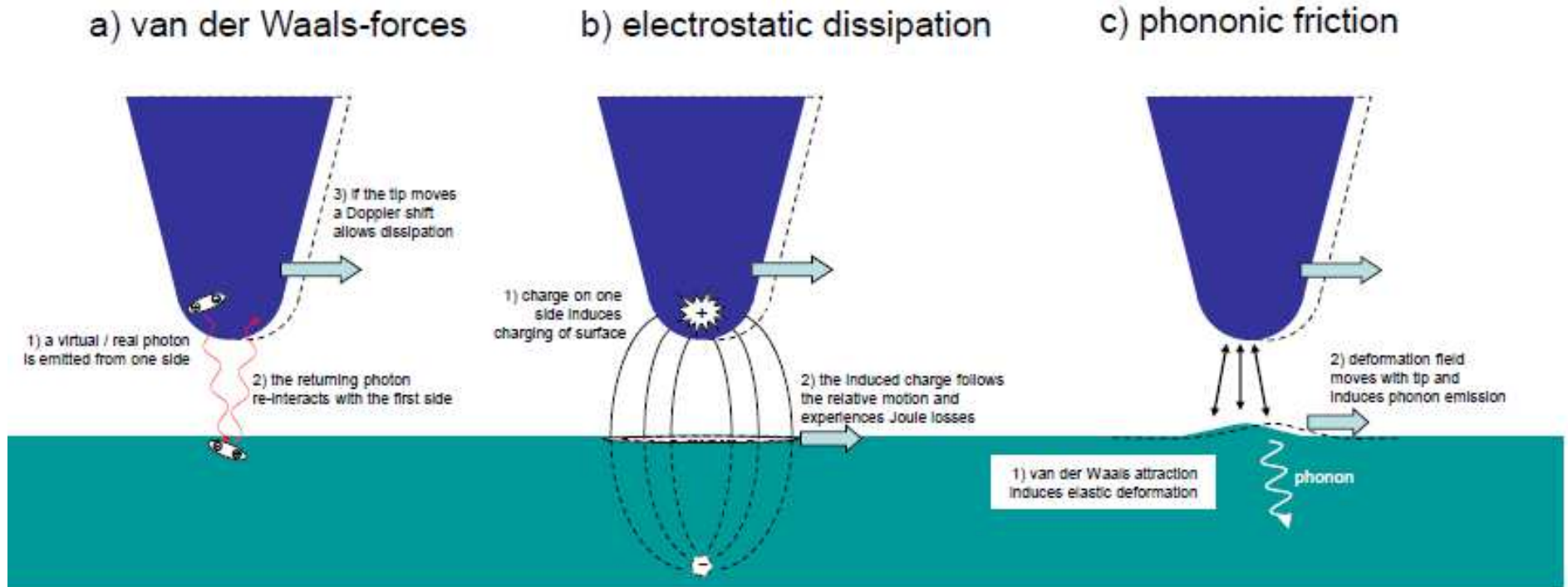
$$\nabla \times \mathbf{E} = i \frac{\omega}{c} \mathbf{B}$$

$$\nabla \times \mathbf{H} = -i \frac{\omega}{c} \mathbf{D} + \frac{4\pi}{c} \mathbf{j}^f$$

$$\left\langle j_i^f(\mathbf{r}) j_k^{f*}(\mathbf{r}') \right\rangle_{\omega} = \frac{\hbar}{(2\pi)^2} \left(\frac{1}{2} + n(\omega) \right) \omega^2 \text{Im} \varepsilon_{ik}(\mathbf{r}, \mathbf{r}', \omega)$$

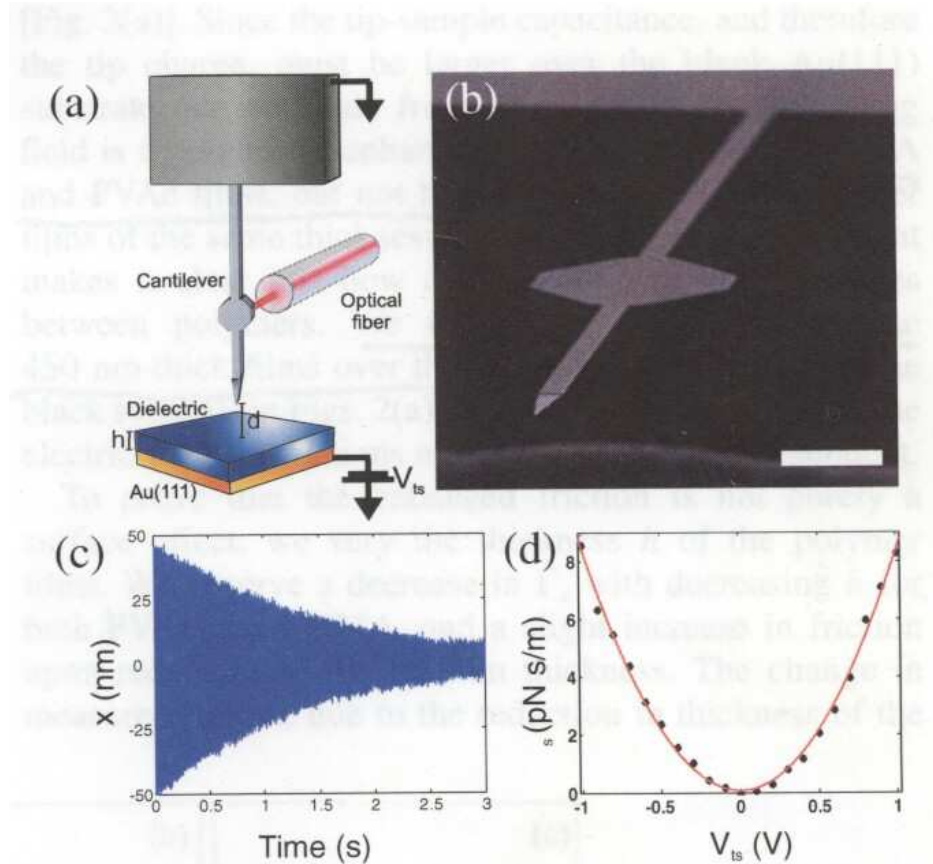
$$n(\omega) = [e^{\hbar\omega/k_B T} - 1]^{-1}$$

Origin of Non-Contact Friction



A.I. Volokitin and B.N.J. Persson, *Rev.Mod.Phys.*, **79**, 1291 (2007)

Non-contact Friction



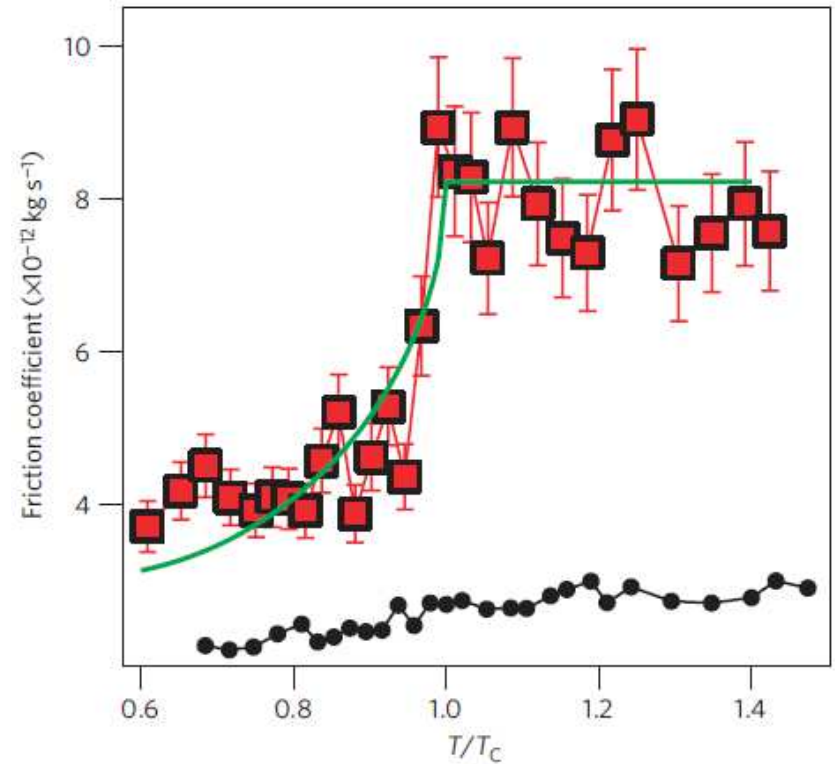
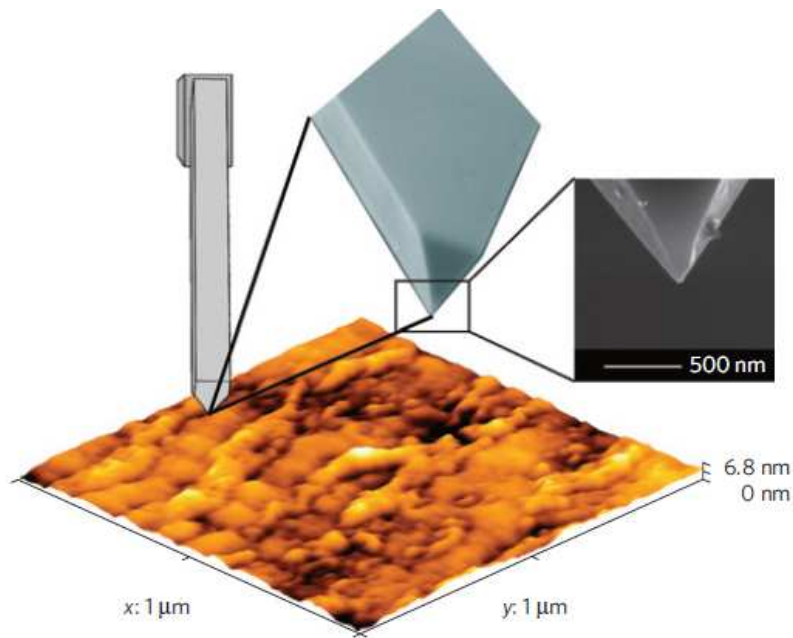
Experiment: **Stipe B.C. *et.al* PRL, 87, 096801 (2001)**

$F_{friction} = \Gamma v$, $\Gamma \sim 10^{-13} - 10^{-12}$ kg/s **at** $d \sim 1 - 100$ nm.

$\Gamma \approx d^{-n}$ **with** $n = 1.3 \pm 0.3$ **and** $n = 0.5 \pm 0.3$, $\Gamma \sim V^2$

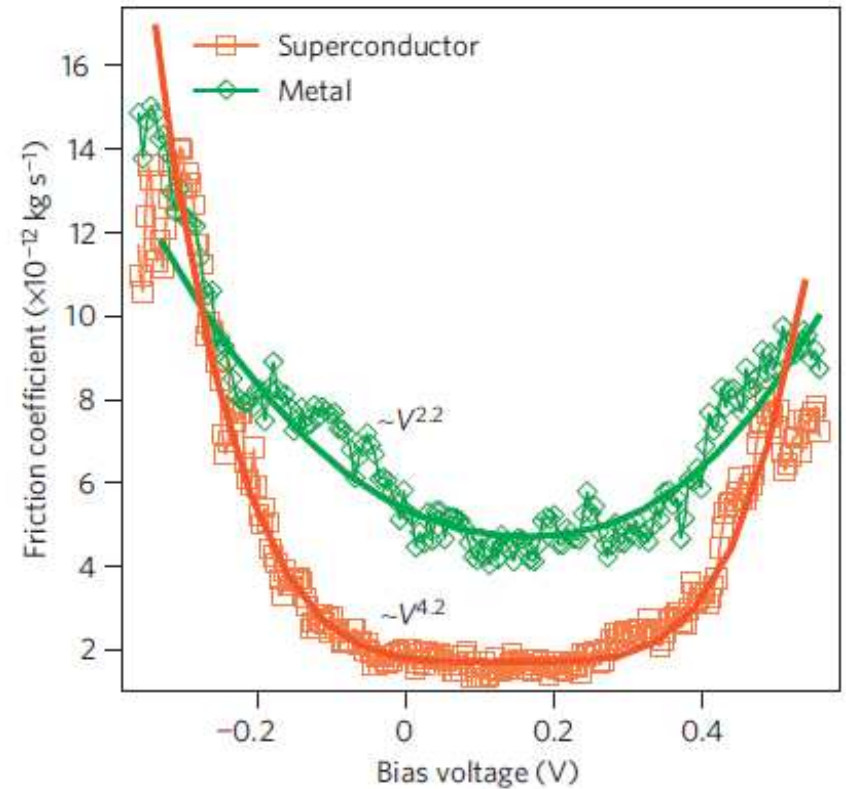
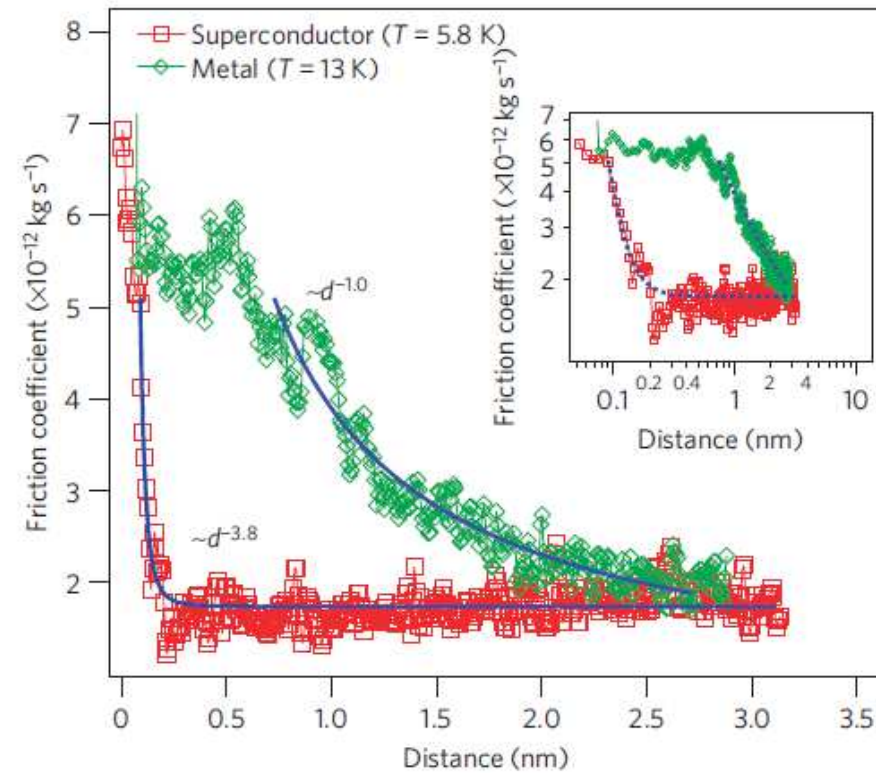
Theory: **A.I. Volokitin and B.N.J. Persson, PRB, 73, 165423 (2006)**

Electronic versus Phononic Friction



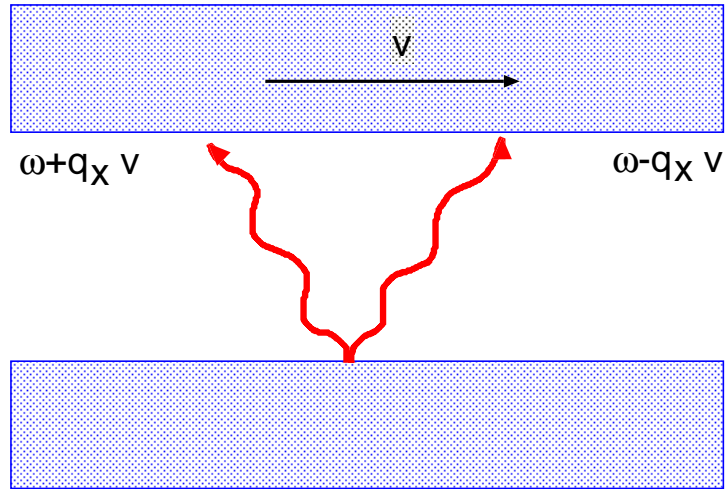
Experiment: M. Kisiel *et.al* *Nat. Materials*, **10**, 119 (2011)

Electronic versus Phononic Friction



Theory: A.I. Volokitin and B.N.J. Persson, *PRB*, **73**, 165423 (2006)

Casimir Friction



Pendry J.B. *JPCM* **9**, 10301 (1997)

A.I. Volokitin and B.N.J. Persson, *JPCM*, **11**, 345 (1999)

Frictional Stress

$$\sigma_{xz} = \int_0^\infty \frac{d\omega}{2\pi} \sum_{i=(s,p)} \int \frac{d^2q}{(2\pi)^2} \hbar q_x \text{sgn}(\omega') (n_2(\omega') - n_1(\omega)) \Gamma_i(\omega, \mathbf{q}),$$

$$\Gamma_i(\omega, \mathbf{q}) = \frac{1}{2k_z |1 - e^{2ik_z d} R_{1i}(\omega) R_{2i}(\omega')|^2} \\ \times \left[(k_z + k_z^*) (1 - |R_{1i}(\omega)|^2) (1 - |R_{2i}(\omega')|^2) \right. \\ \left. + 4(k_z - k_z^*) \text{Im} R_{1i}(\omega) \text{Im} R_{2i}(\omega') e^{-2d \text{Im} k_z} \right]$$

$$\omega' = \omega - q_x v, \quad n_i(\omega) = [\exp(\hbar\omega/k_B T_i) - 1]^{-1}, \quad k_z = \sqrt{(\omega/c)^2 - q^2}$$

A.I. Volokitin and B.N.J. Persson, *JPCM*, **11**, 345 (1999)

Small Velocities

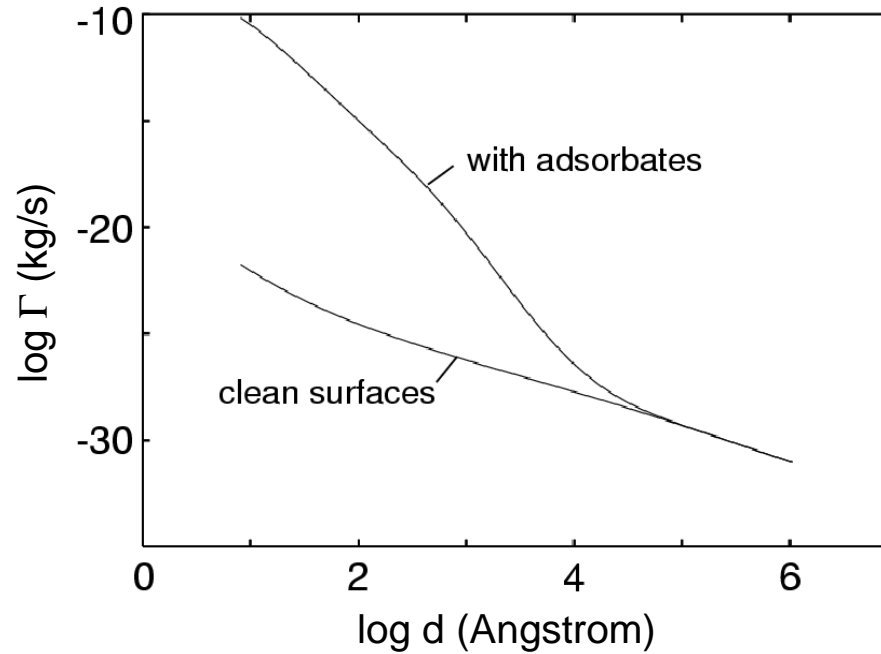
$$v \ll v_T = k_B T d / \hbar, \quad d \ll \lambda_T = c \hbar / k_B T,$$

$$\sigma_{xz} = \gamma v,$$

$$\gamma = \frac{\hbar^2}{8\pi^3 k_B T} \int_0^\infty \frac{d\omega}{\sinh(\hbar\omega/k_B T)} \sum_{i=p,s} \int d^2 q q_x^2 e^{-2qd}$$
$$\times \frac{\text{Im} R_{1i}(\omega) \text{Im} R_{2i}(\omega)}{|1 - e^{-2qd} R_{1i}(\omega) R_{2i}(\omega)|^2},$$

$$\Gamma = \int dS \gamma(z(x, y))$$

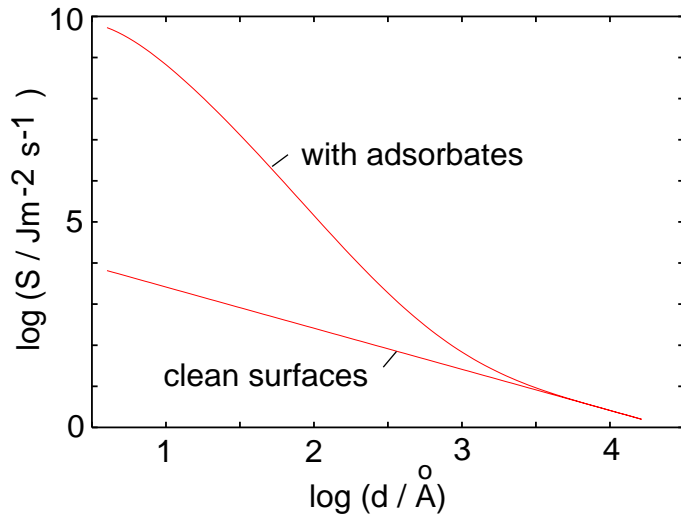
Adsorbate enhancement of Casimir friction



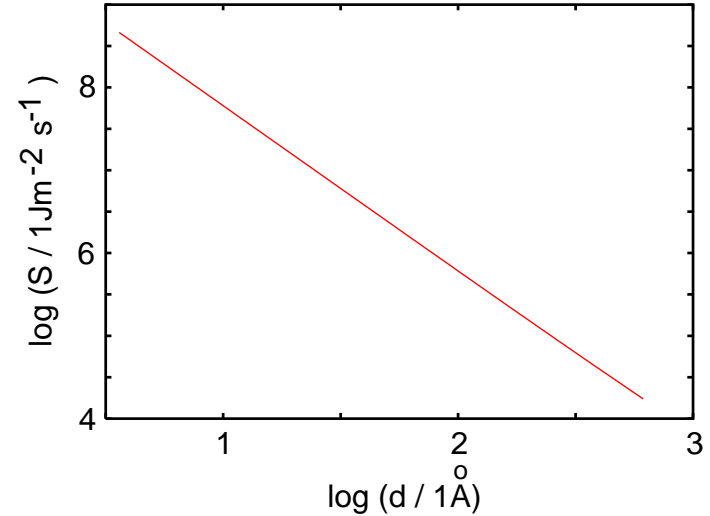
Cs/Cu(100)

A.I. Volokitin and B.N.J. Persson, *PRB*, **73**, 165423 (2006)

Radiative Heat Transfer.



K/Cu(001)

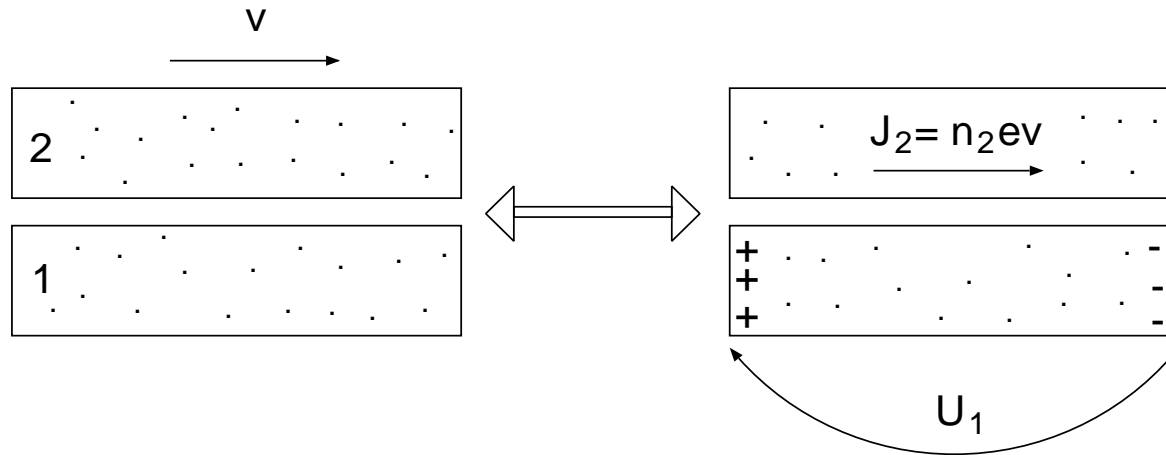


SiC

$$T_1 = 273 \text{ K}, T_2 = 0 \text{ K}$$

Volokitin A.I. and Persson B.N.J. *PRB*, **69**, 045417 (2004)

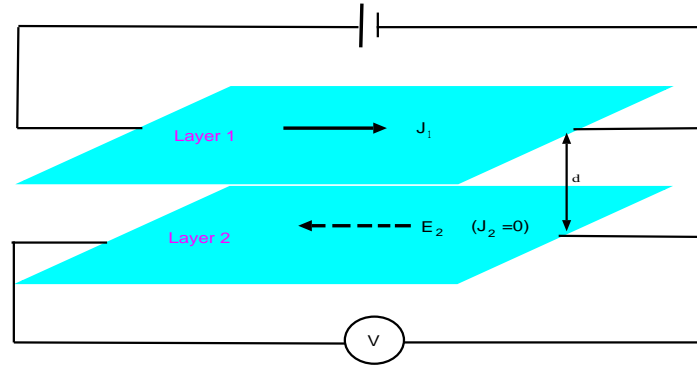
Two ways to study Casimir friction



Left: Upper block is sliding relative to block at the bottom

Right: The current is induced in the upper block .

Frictional Drag in 2D-systems



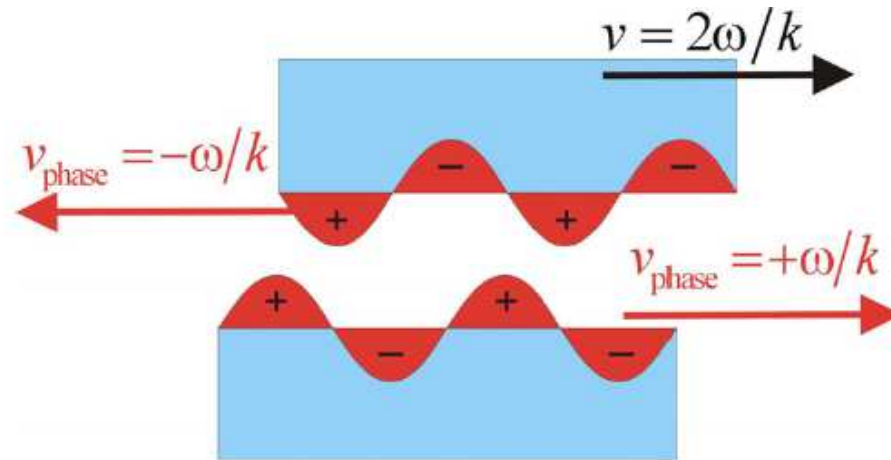
Theory - Coulomb Drag. M. B. Pogrebenskii
Sov.Phys.Second., **11** (1977) 372, P. J. Price *Physica*
B+C, **117** (1983) 750

Experiment - Quantum wells T. J. Gramila *et.al PRL*, **66**
(1991) 1216, U. Sivan *et.al PRL*, **68** (1992) 1196

Experiment - Graphene Sheets S. Kim *et.al PRB*, **83** (2011)
161401, R.V. Gorbachev *et.al Nat.Phys.*, **8** (2012) 896

Theory - Casimir Friction. A.I. Volokitin and B.N.J. Persson,
J.Phys.:Condens.Matter, **13**, 859 (2001); *ibid, EPL* **103**
24002 (2013)

Quantum Friction



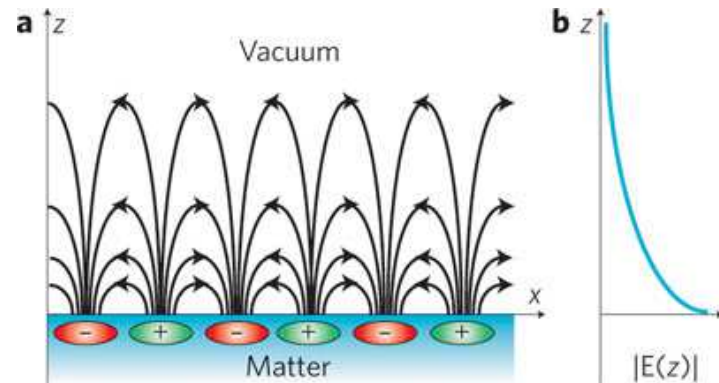
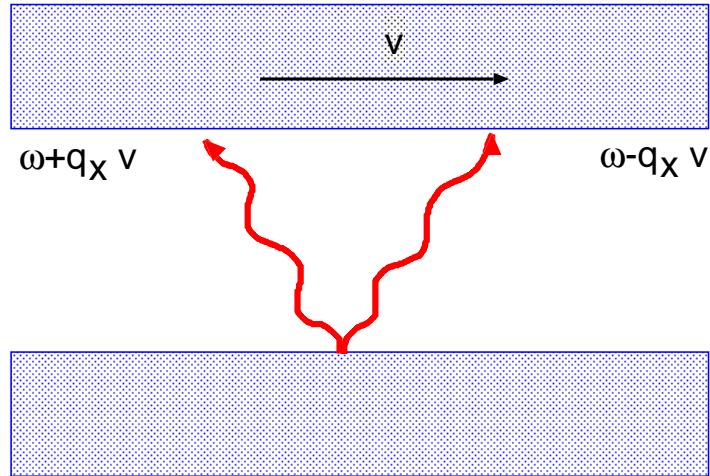
$$q_x v = \omega_1 + \omega_2$$

Pendry J.B. *JPCM* **9**, 10301 (1997)

Volokitin A.I. and Persson B.N.J. *JPCM*, **11**, 345 (1999)

Volokitin A.I. and Persson B.N.J. *PRB*, **78**, 155437 (2008)

Anomalous Doppler Effect



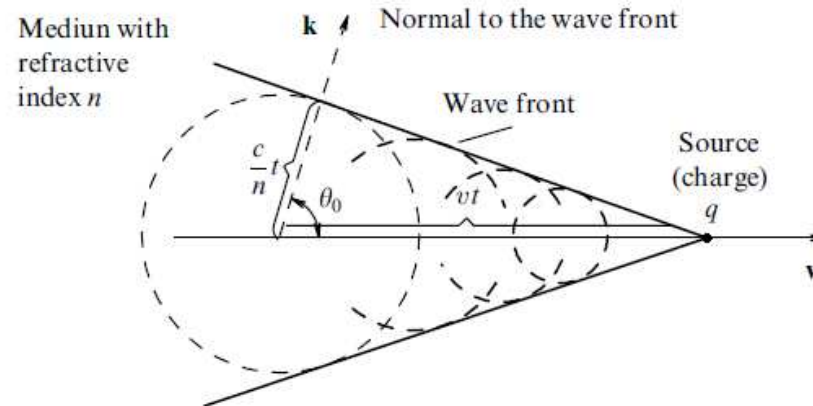
Normal Doppler effect $\omega' = \omega - q_x v > 0$

Anomalous Doppler effect $\omega' = \omega - q_x v < 0$

Thermal fluctuations dominate at $v < v_T = k_B T d / \hbar$

Quantum fluctuations dominate at $v > v_T = k_B T d / \hbar$

Classical Vavilov-Cherenkov Radiation

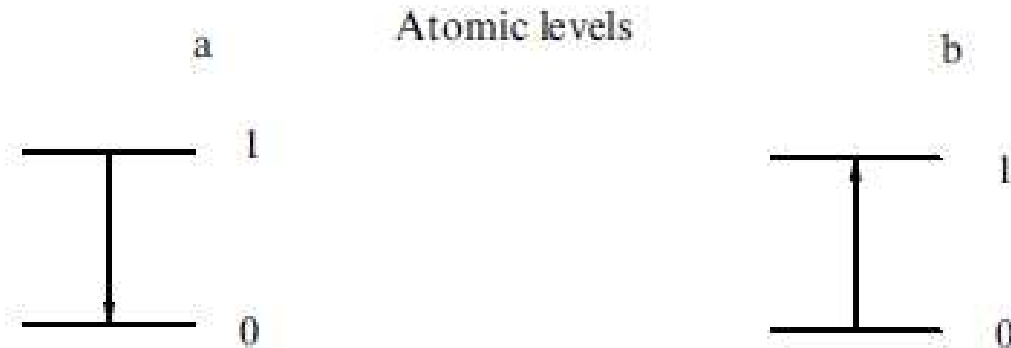


Cherenkov P.A. *Dokl. Akad. Nauk SSSR*, **2**, 451 (1934)

Resonant condition: $q_x v = cq/n > v_0 = cq_x/n$

Threshold velocity: $v > c/n$

Quantum Vavilov-Cherenkov Radiation

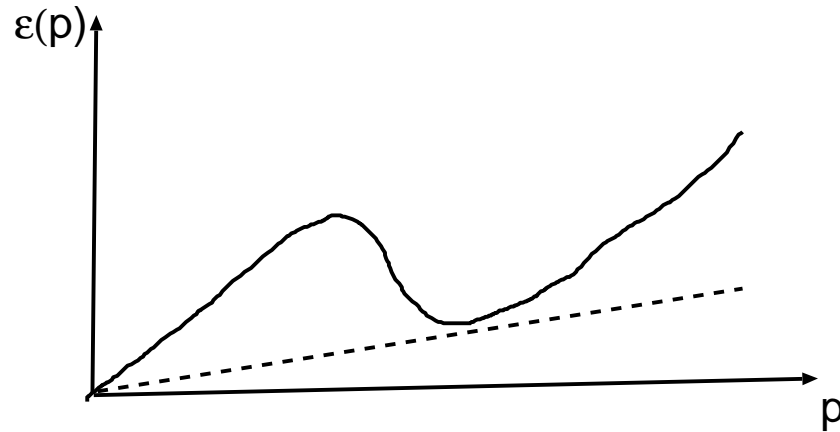


Frank M.I. *J.Phys.USSR*, 7, 49 (1943)

Doppler effect (a): $\omega_{ph} = \omega_0 - g_x v > 0$

Doppler effect (b): $\omega_0 - g_x v < 0; \omega_{ph} = g_x v - \omega_0$

The Landau criterion for the critical velocity of a superfluid



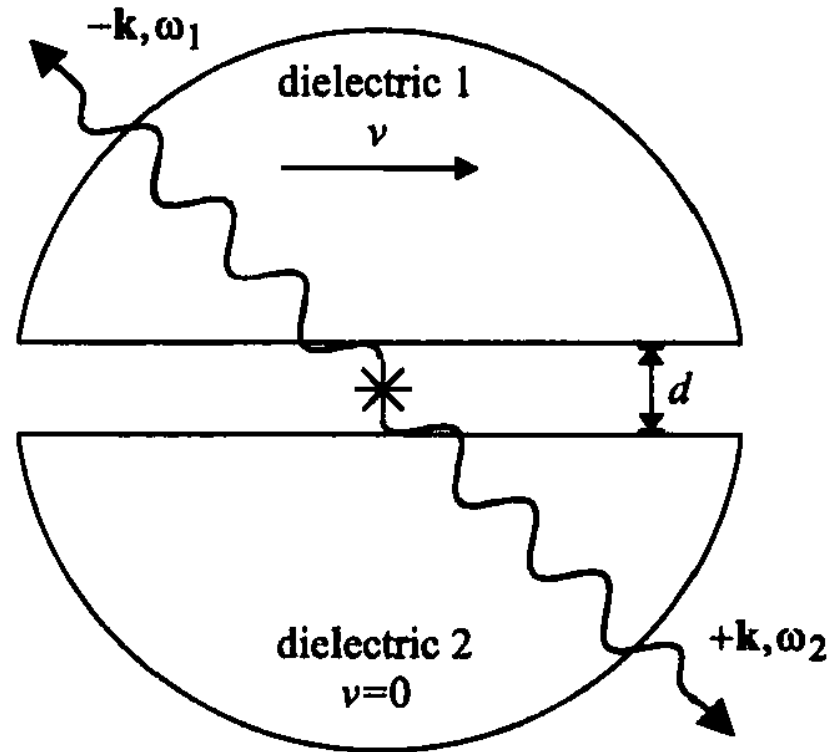
$$E = \frac{Mv^2}{2} + \varepsilon(p) - pv$$

$$\varepsilon(p) - pv < 0$$

$$v > v_c = \min \left(\frac{\varepsilon(p)}{p} \right)$$

Landau L.D., *Zh. Eksp. Teor. Fiz.* 11, 592 (1941)

Radiation at shearing two transparent plates

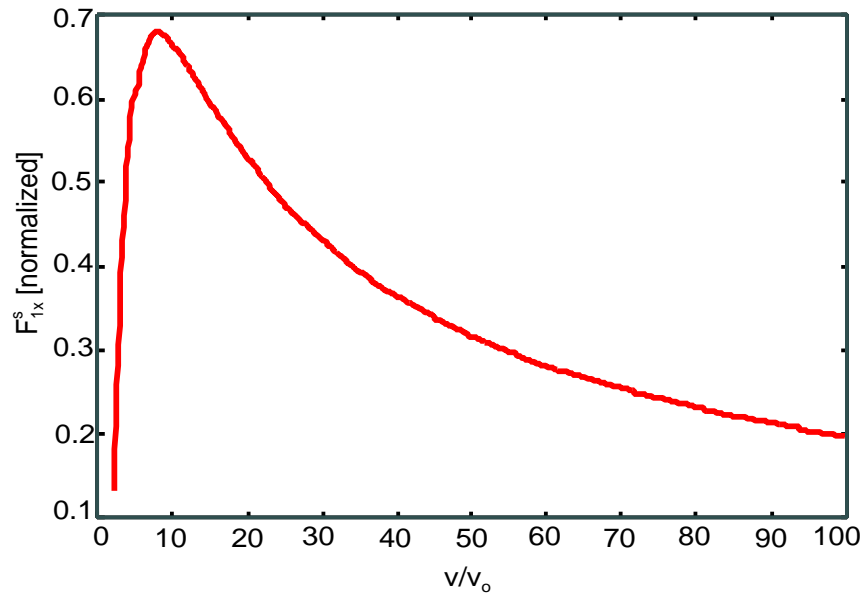


Pendry J.B. *JMO* **45**, 2389 (1998).

Magreby F.M., Golestian R., and Kardar M., *PRA* **88**, 042509 (2013).

Volokitin A.I. and Persson B.N.J. *PRB* **93**, 035407 (2016).

Non-Relativistic Theory



Resonant condition: $\omega_{ph} = q_x v - cq/n = cq/n, v > v_0 = 2c/n$

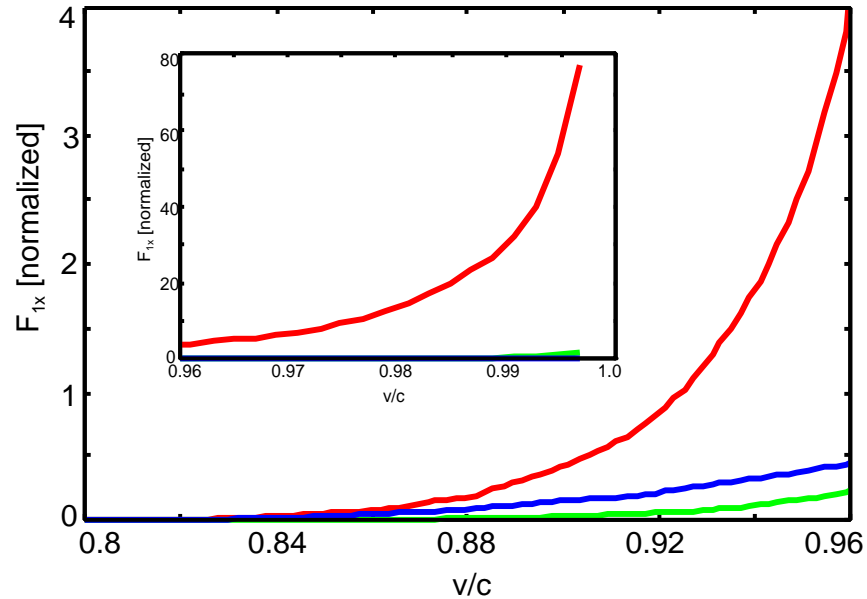
$$F_{1x}^s = \frac{\hbar v_0}{\pi^3 d^4} F_{1x}^s [\text{normalized}]$$

$$R_s = \frac{\sqrt{(\omega/c)^2 - q^2} - \sqrt{(n\omega/c)^2 - q^2}}{\sqrt{(\omega/c)^2 - q^2} + \sqrt{(n\omega/c)^2 - q^2}}$$

Magreby F.M., Golestian R., and Kardar M., *PRA* **88**, 042509 (2013).

Volokitin A.I. and Persson B.N.J. *PRB* **93**, 035407 (2016).

Relativistic Theory

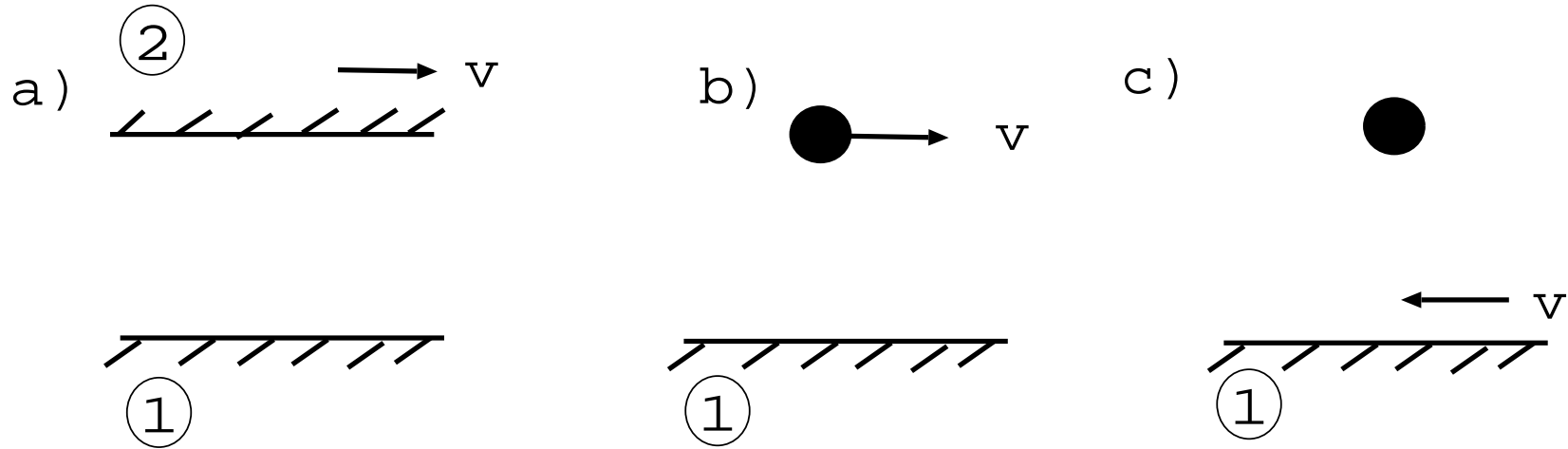


$$\omega_{ph} = q_x v - cq'/\gamma n = cq/n, v > v_0 = 2cn/(n^2 + 1)$$

Volokitin A.I. and Persson B.N.J. *PRB* **78**, 155437 (2008)

Volokitin A.I. and Persson B.N.J. *PRB* **93**, 035407 (2016).

Radiation From Moving Neutral Particle

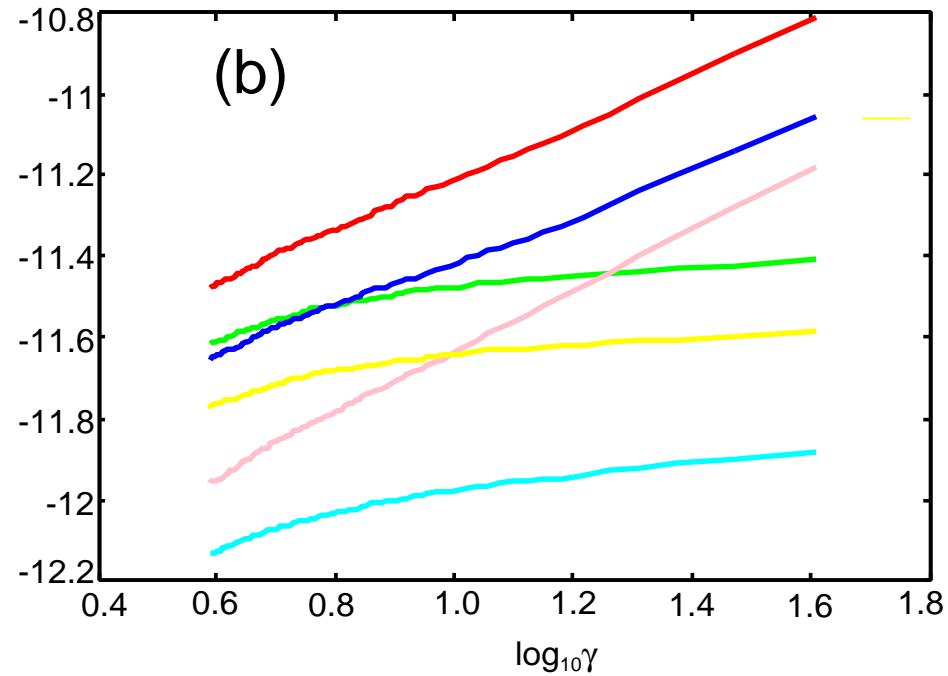
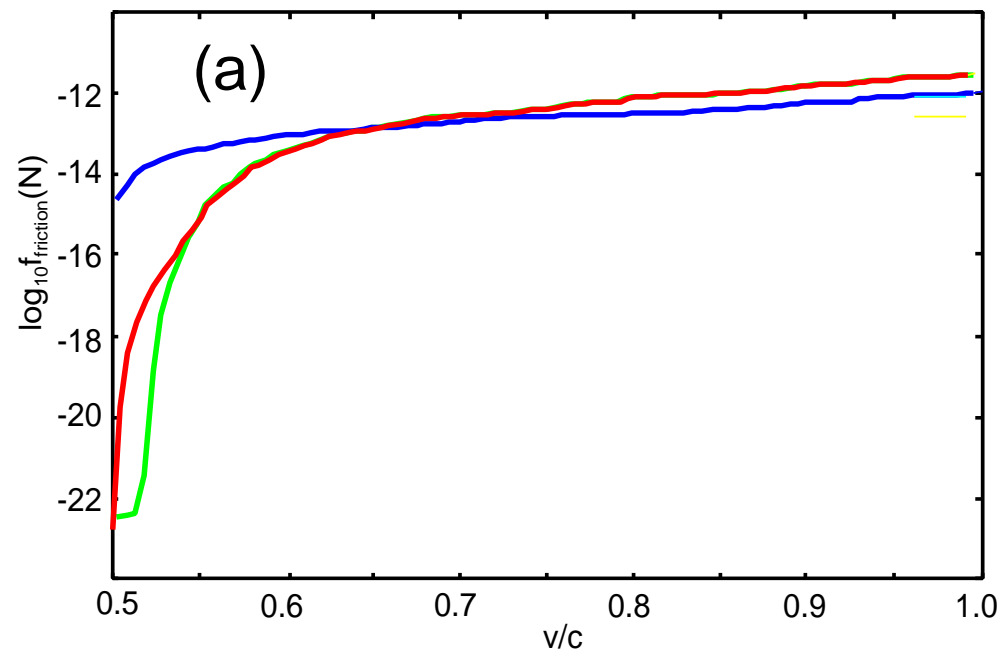


$$\omega_{ph} = q_x v - \omega_0 / \gamma = cq/n, v > v_0 = c/n$$

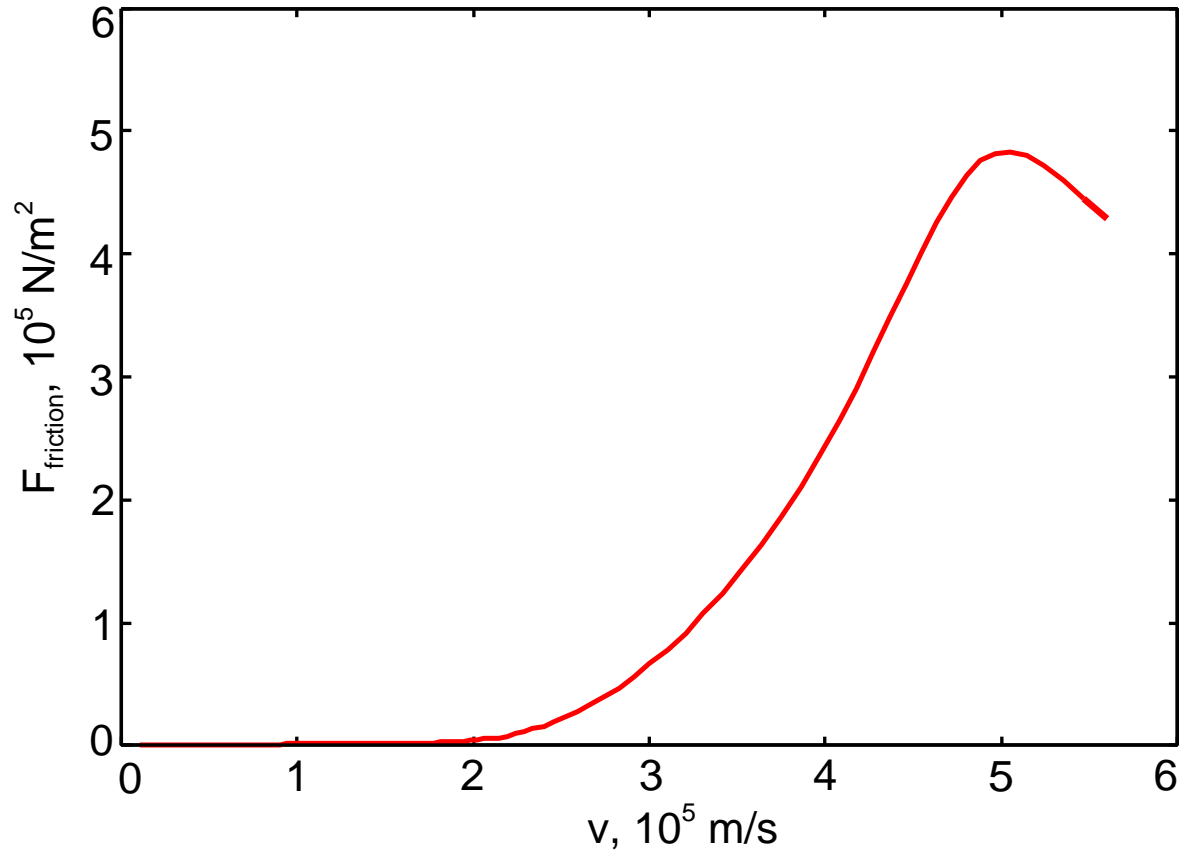
Pieplow G. and Henkel C., *JPCM* **27**, 035407 (2015).

Volokitin A.I. and Persson B.N.J. arxiv.org/abs/1512.04366 (2016).

Quantum Friction for Particle



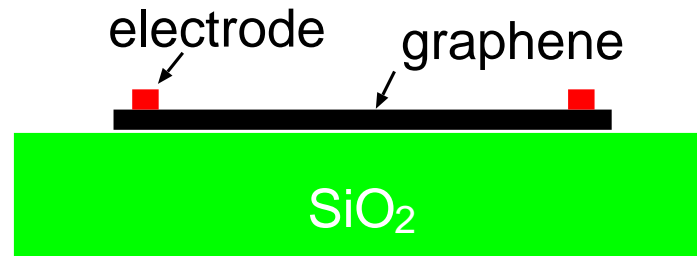
Polar Dielectric SiO₂



Resonant condition: $\omega_{ph} = q_x v - \omega_0 = \omega_0$

Threshold velocity: $v > 2\omega_0 / q_{xmax} \sim 2\omega_0 d \sim 2 \cdot 10^5 \text{ m/s}$

Graphene on SiO₂



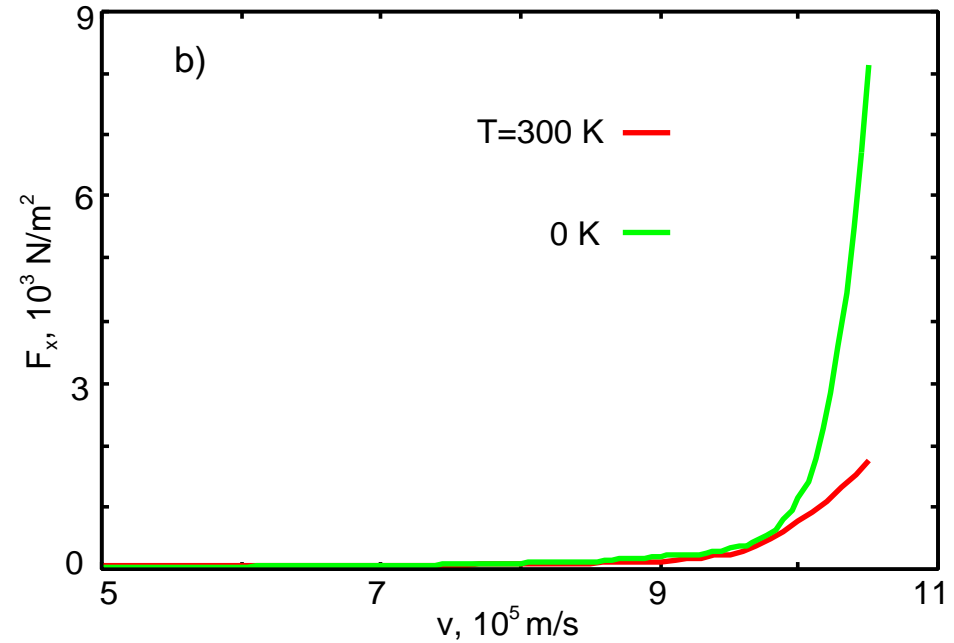
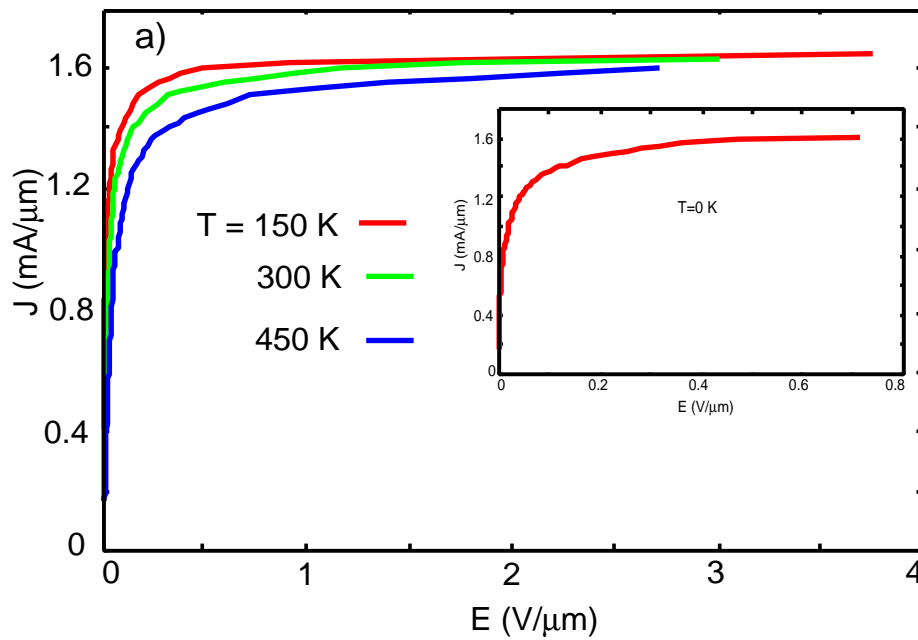
Threshold velocity: $v > v_F + \omega_0/q_{xmax} \approx v_F \sim 10^6 \text{m/s}$

Resonant condition: $\omega_{ph} = q_x v - v_F q = \omega_0$

Experiment: Freitag M., Steiner M., Martin Y., Perebeinos V., Chen Z., Tsang J.C., and Avouris P., *Nano Lett.* **9**, 1883 (2009).

Theory: Volokitin A.I. and Persson B.N.J. *PRL* **106** 094502 (2011)

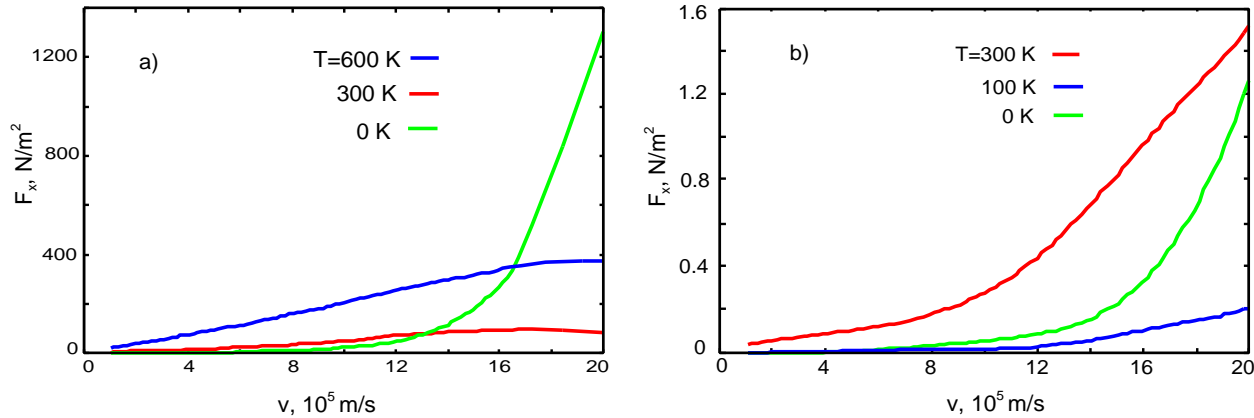
Current density-electric field dependence in graphene on SiO₂



$$v_{sat} \sim v_F \sim 10^6 \text{ m/s}$$

$$J_{sat} = en_s v_{sat} \sim 1 \text{ mA}/\mu\text{m}$$

Frictional Drag between Graphene Sheets



$d=1$ nm

$d=10$ nm

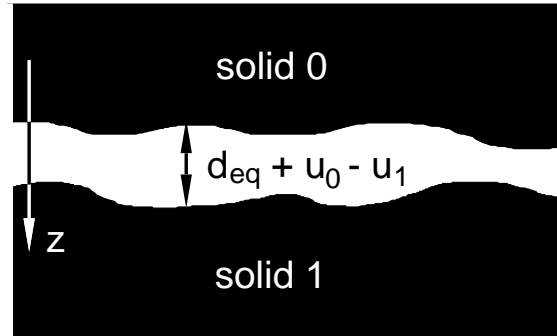
At $v \ll v_F$ induced electric field $E = \rho_D J = \mu^{-1} v$.

$$\rho_D = \frac{\Gamma}{(ne)^2} = \frac{h}{e^2} \frac{\pi \zeta(3)}{32} \left(\frac{k_B T}{\epsilon_F} \right)^2 \frac{1}{(k_F d)^2} \frac{1}{(k_{TF} d)^2},$$

$$F_{x0} = \frac{\hbar v}{d^4} \frac{15 \zeta(5)}{128 \pi^2} \left(\frac{v}{v_F} \right)^2 \frac{1}{(k_{TF} d)^2}.$$

Volokitin A.I. and Persson B.N.J. *EPL* **103** 24002 (2013)

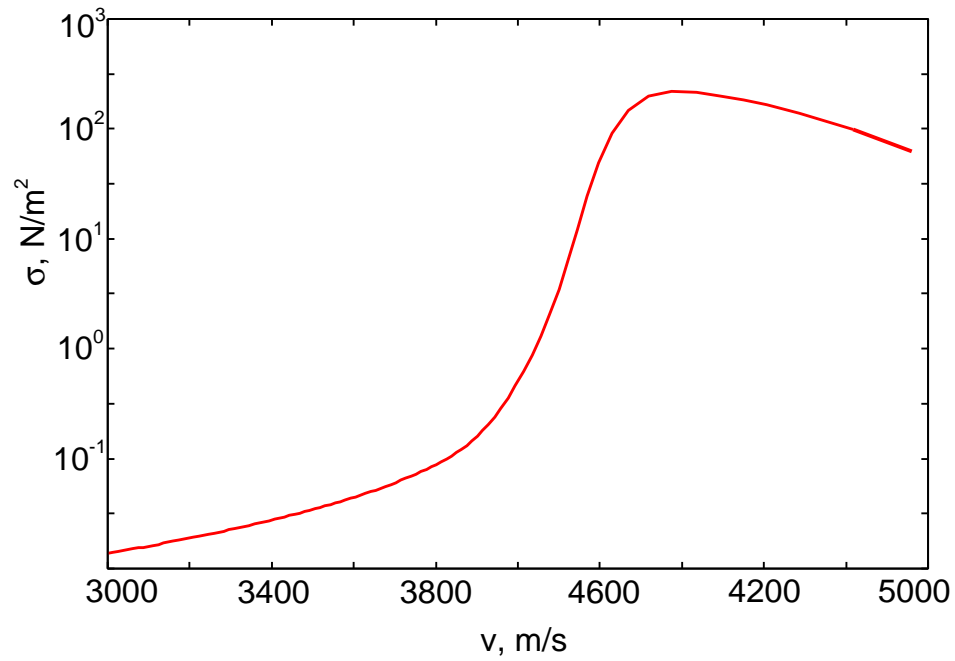
Acoustic Phonon Emission



$$\sigma(\mathbf{x}, t) = K[u_0(\mathbf{x} - \mathbf{v}t, t) - u_1(\mathbf{x}, t)],$$

Persson B.N.J., Volokitin A.I. and Ueba H., *JPCM* **23**
045009 (2011)

Acoustic Phonon Emission



Summary

- Casimir friction can be studied using modern experimental setups for observation of frictional drag in graphene systems..
- The challenging problem is to study frictional drag for graphene for strong electric field (large drift velocity) when Casimir friction is dominated by quantum fluctuations (quantum friction).
- The challenging problem for experimentalists is to develop setup for mechanical detection of Casimir friction using AFM.
- Quantum friction is strongly enhanced above the threshold velocity.
- The threshold velocity is determined by a type of excitations which are responsible for quantum friction.