



# Surface phonon polaritons supported heat conduction

**Thomas Antoni**

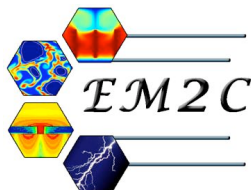
Laurent Tranchant



José Ordóñez-Miranda

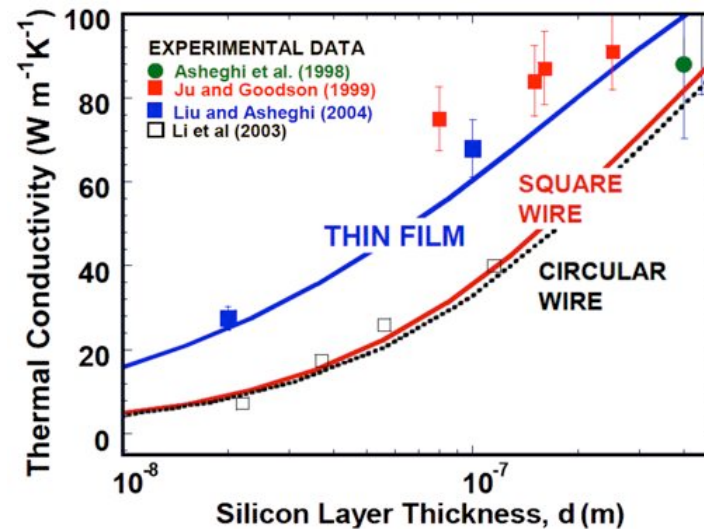


Sebastian Volz



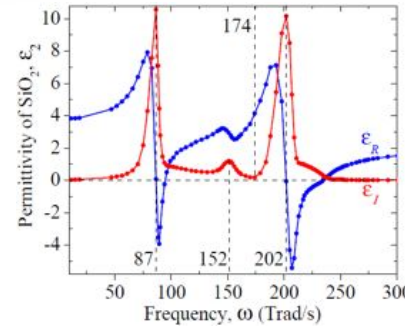
*Nanoscale Radiative Heat Transfer - Physique School Les Houches 2013*

- **Downscaling of nanosystems tend to be limited by heat extraction**
- **Bulk thermal conductivity decreases with material size**

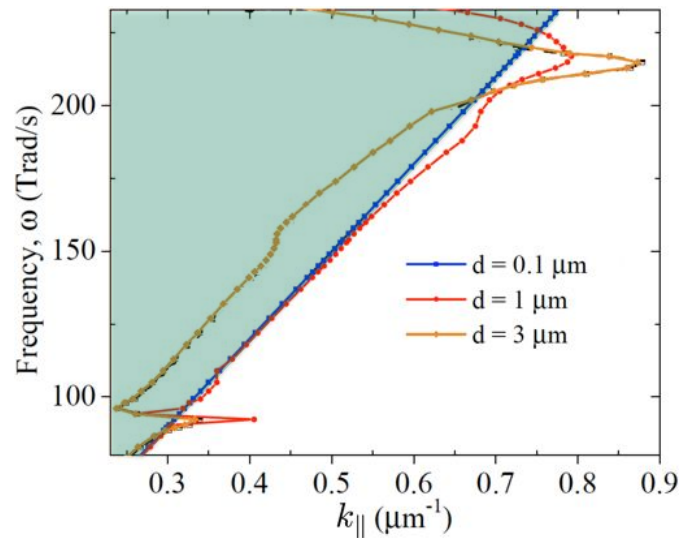
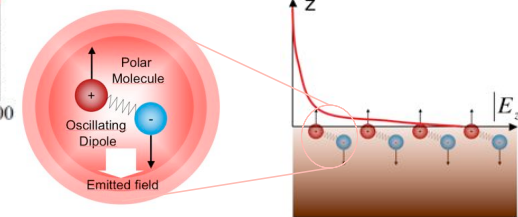


- **But nanosystems have very high surface/volume ratio**
- **Use surface effects to extract heat**

- **Happens at the interface of polar materials and dielectrics**
- **Superposition of photon and phonon state**



E. Palik, Handbook of Optical Constants in solids (1985)



- **Part of the dispersion under the light line**

$$k_{\parallel} \geq \omega/c \Leftrightarrow k_{\perp} = i\sqrt{k_{\parallel}^2 - \omega^2/c^2}$$

- **Wavelength ~ 10 μm, corresponding to max of Planck's law at ambient**



- **We look at the propagation of the SPhP**

- **Good thing about nanosystems is that analytical calculations can be performed**

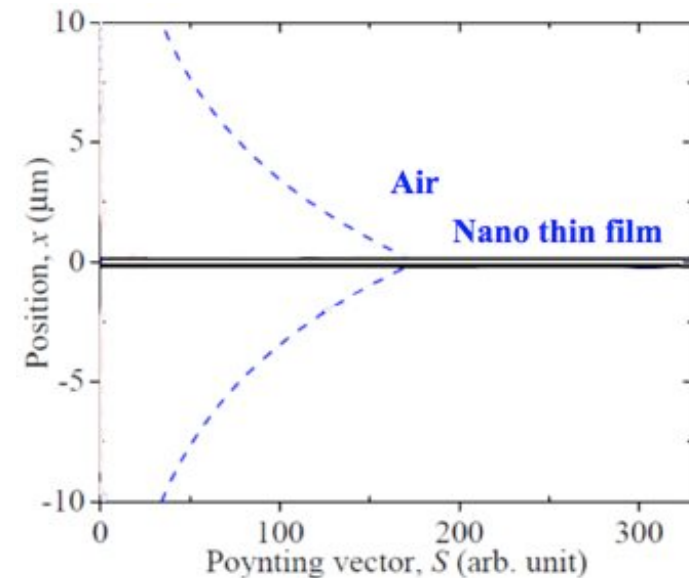
$$\varepsilon_1 \in \mathbb{R}$$

$$\varepsilon_2 \in \mathbb{C}$$



- **Perturbative calculations for  $k_{1,\perp}d \ll 1$** 
  - For SPhP @ 9  $\mu\text{m}$  ( $\text{SiO}_2$ ),  $d \sim 300 \text{ nm}$

- **Poynting vector:**



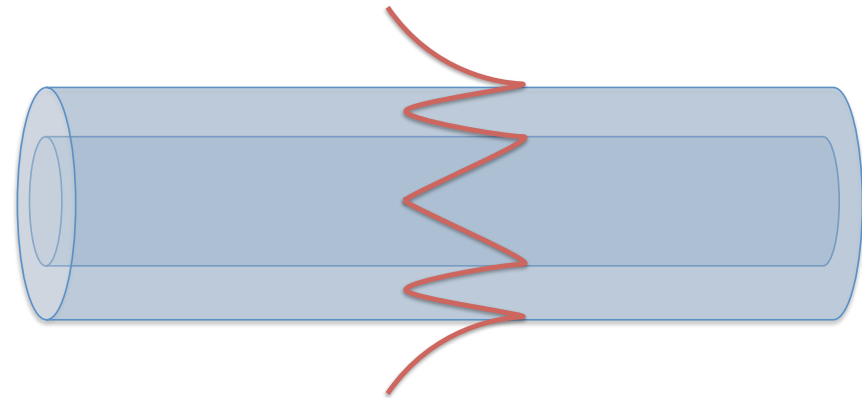
- **Thermal conductivity contribution of SPhP**

$$\kappa = \frac{1}{4\pi d} \int_0^\infty k_{\parallel} \Lambda \hbar \omega \frac{\partial}{\partial T} \frac{1}{e^{\frac{\hbar\omega}{k_B T}} - 1} d\omega$$

D. Chen *et al.*, PRB **72**, 155435 (2005)

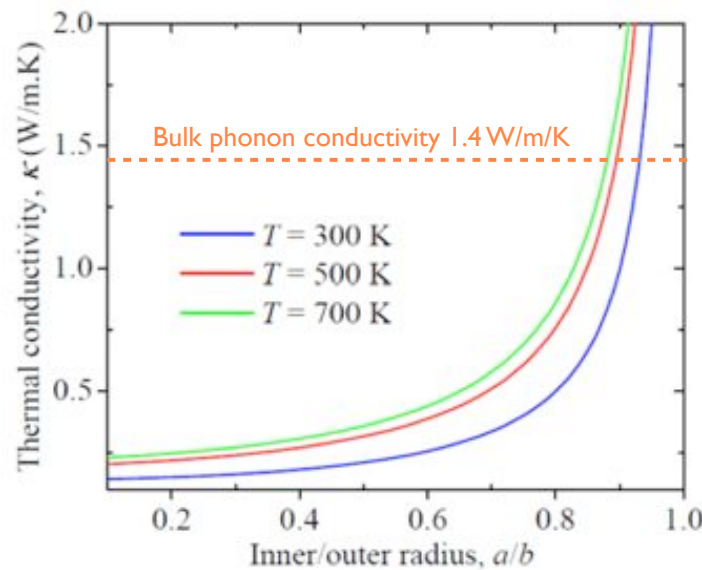
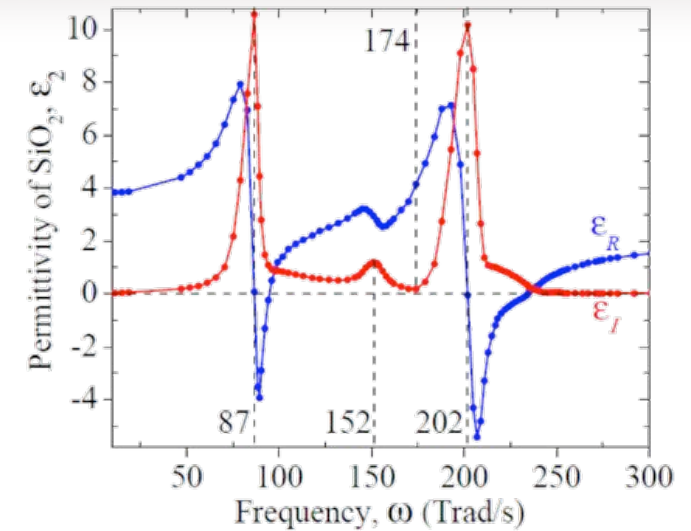
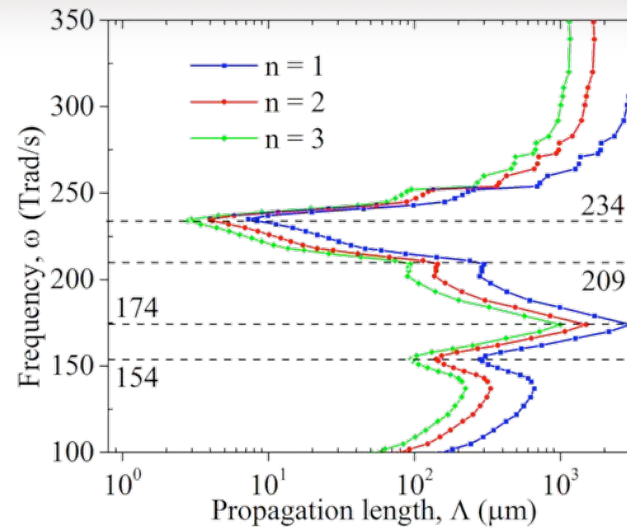
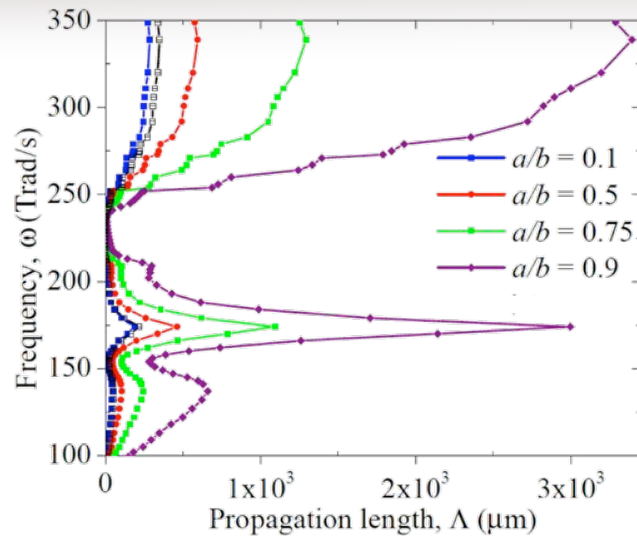
- **Only the propagation length  $\Lambda$  determines the thermal conductivity**

- **2D systems**
- **Coupling of radial modes**
- **Lot of angular modes**
- **For  $k_{1,\perp}d \ll 1$ , the sole parameter is the inner to outer radius ratio**
- **SiO<sub>2</sub> widely used in microfabrication**



# Analytical results

## On SiO<sub>2</sub> nanotubes



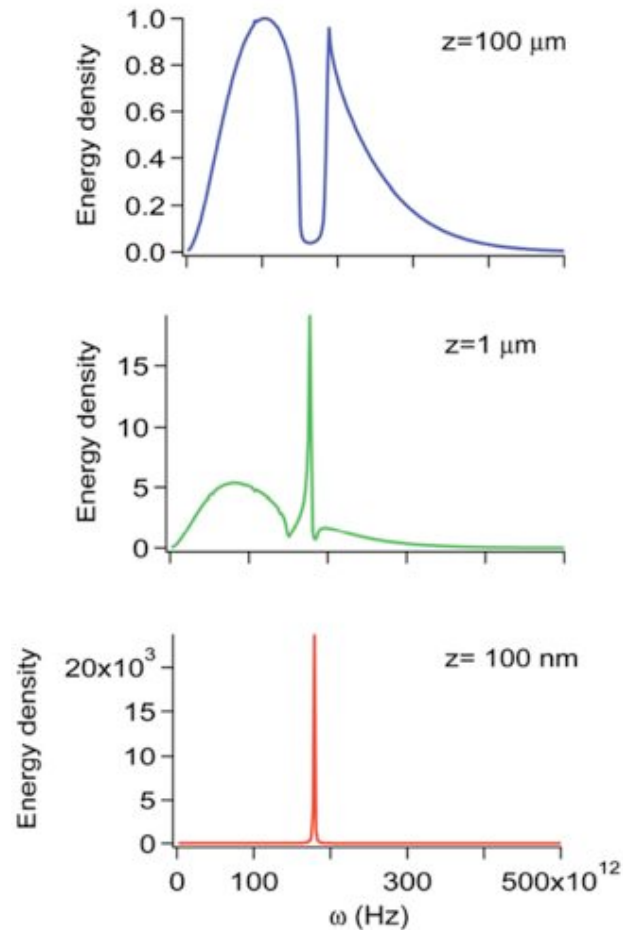
- **For large radii radio SPHP contribution > bulk**

- **Typical sizes**

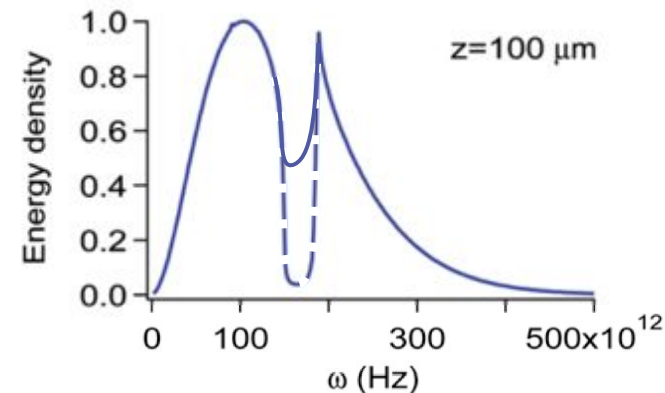
- Outer radius 3 μm
- Thickness 300 nm

J. Ordonez-Miranda et al., JAP  
113, 084311 (2013)





- **In the far field, the existence of the SPhP gives a dip in the emission**
- **If SPhP are diffracted, this dip will decrease**



K. Joulain et al.,  
*Surface Science*  
Report **57** (3), 2005

- **SPhP stand below the light cone, they are not radiated**
  
- **Usual schemes to couple SPhP:**
  - Grating
  - Internal total reflexion in prism
  
- **But the tube diffracts by itself!**

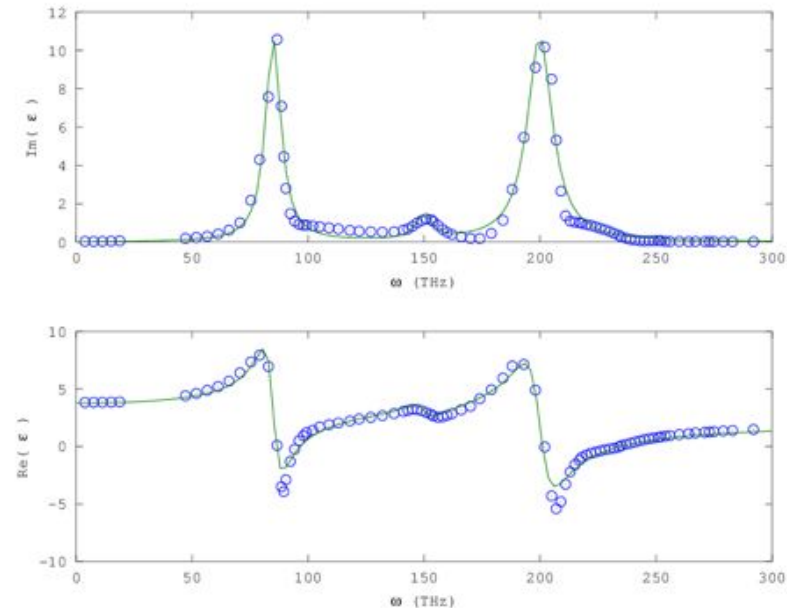
- **Finite Difference in Time Domain**

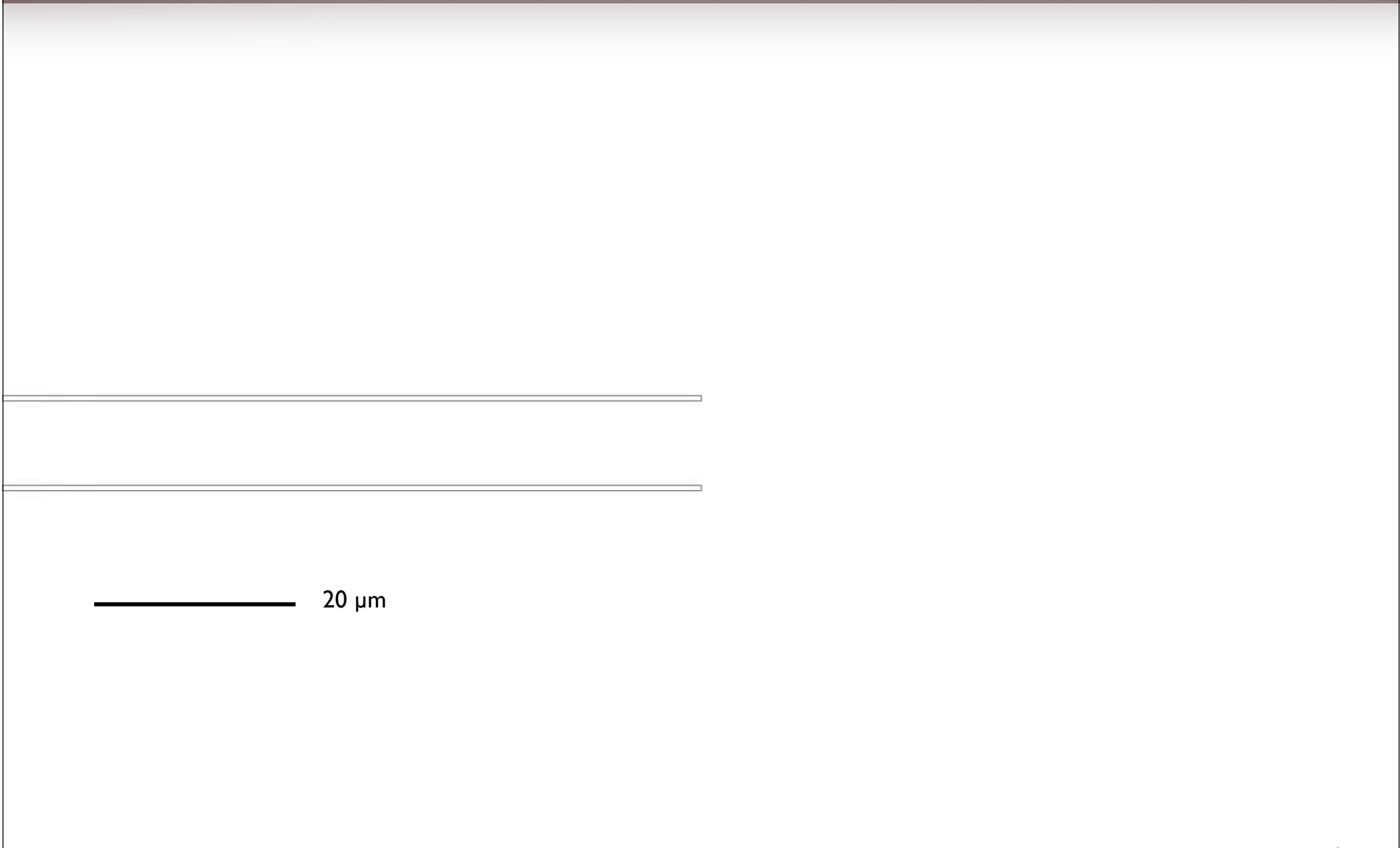
- Discretization of space and time
- Polychromatic sources
- Arbitrary systems shape

- **Lorentz model for SiO<sub>2</sub>**

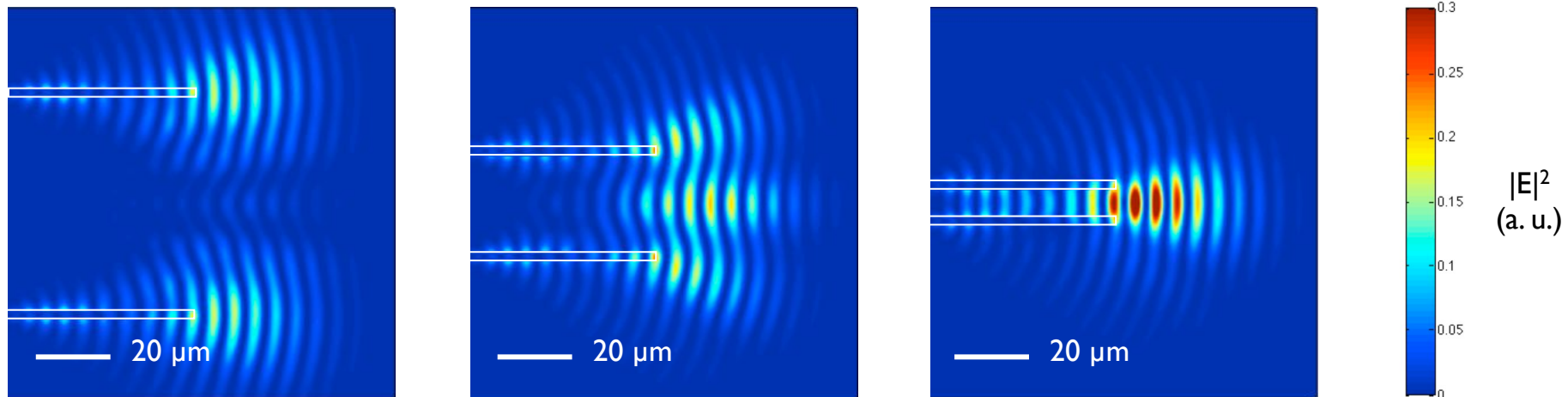
$$\varepsilon(\omega) = \varepsilon_{\infty} + \sum_{j=1}^3 \frac{\sigma_j \omega_j^2}{\omega_j^2 - \omega^2 - i\Gamma_j \omega}$$

MEEP code



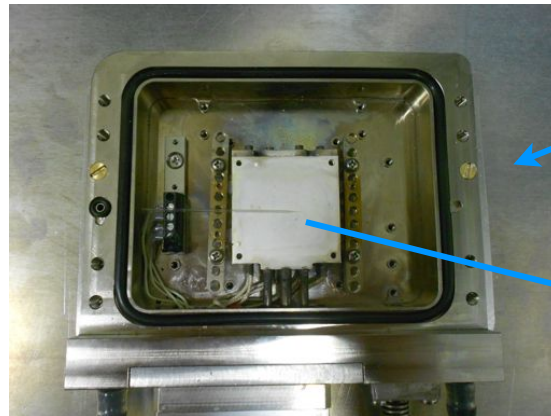


————— 20  $\mu\text{m}$



- **For radii  $\sim \lambda_{\text{SPHP}}$  both sides of the tube interfere constructively and emits on a narrow angle cone  $30^\circ$ , compatible with standard Cassegrain objectives NA**

- **FTIR bench + IR microscope**



- **Use of SPhP to increase longitudinal conductivity in SiO<sub>2</sub> nanotubes**
- **Analytical computation shows the possibility to double the total conductivity**
- **FDTD simulation of SPhP diffraction in far field with nanotube**
- **Now looking for the spectral signature of SPhP in far field with FTIR measurement**